

Calculus AB

P-3 Functions

function - a rule or a map that assigns each value of the domain to exactly one value of the range

domain - set of all possible inputs



range - set of all possible outputs.



Transformations

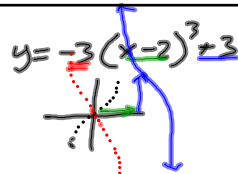
$$y = a(bx - c) + d$$

$a \rightarrow$ vertical stretch or compression

$b \rightarrow$ horizontal stretch or compression

$c \rightarrow$ horizontal translation $(-\frac{c}{b})$

$d \rightarrow$ vertical translation



Evaluate the function. Determine its domain and range.
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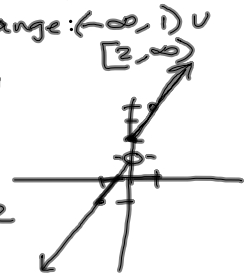
$$27) f(x) = \begin{cases} 2x+1, & x < 0 \\ 2x+2, & x \geq 0 \end{cases} \quad \begin{array}{l} \text{domain: } \mathbb{R} \\ \text{range: } (-\infty, 1) \cup [2, \infty) \end{array}$$

a) $f(-1) = 2(-1) + 1 = -1$

b) $f(0) = 2(0) + 2 = 2$

c) $f(2) = 2(2) + 2 = 6$

d) $f(t^2 + 1) = 2(t^2 + 1) + 2 = 2t^2 + 4$



Sketch a graph of the function and find its domain and range.

35) $f(x) = \sqrt{9 - x^2}$ $[-3, 3]$



$[0, 3]$

Determine whether y is a function of x .

45) $x^2 + y^2 = 4$ no

Find the composite functions $(f \circ g)$ and $(g \circ f)$.
What is the domain of each composite function?
Are the two functions equal?

61) $f(x) = x^2$
 $g(x) = \sqrt{x}$

$(f \circ g)(x) = f(g(x))$

$= f(\sqrt{x})$

$= (\sqrt{x})^2 = x$

$(g \circ f)(x) = g(f(x))$

$g(x^2) = \sqrt{x^2} = |x|$

Assignment:

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2-30 even

31 - 38 all, just domain and range,

41 - 54 all,

59 - 65 odd,

66, 70, 72,

97a, 97b, 98